## **Granular Soft Computing:** A Paradigm in Information Processing

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## Granular computing (GrC): Outline

- Granular Spaces
- Fuzzy granulation
- Rough granulation
- Wavelet granulation
- Neural Granulation
- Basic issues
- Hybrid granular spaces
- Application to pattern classification
- Concluding remarks

### **Granular spaces**

- ≻ Time
- Frequency
- Time-frequency
- > Transformation
- Neural space

## **Historical notes**

### Main driving force of GrC

- Fuzzy set, and
- Rough set theories

However, the connections to other fields and the generality, flexibility, and potential of GrC have not been fully explored, such as

- Wavelet transform and others
- Neural networks

## Concept of Flexibility Analysis

## Fuzzy Sets and Information Granules : Basic Concepts



### **FUZZY LOGIC—A BRIEF SUMMARY**

Misconceptions about fuzzy logic. Fuzzy logic is not fuzzy, In essence, fuzzy logic is a precise logic of imprecision.

The nucleus of fuzzy logic, is the concept of a fuzzy set.

EXAMPLE: Age of a person Young, Old

### The concept of Fuzzy set (ZADEH 1965)



Informally, a fuzzy set, A, in a universe of discourse, U, is a class with a fuzzy boundary .

### Fuzzy logic...

- A set, A, in U is a class with a crisp boundary.
- A set is represented through association with a characteristic function c<sub>A</sub>: U {0,1}
- A fuzzy set is represented through graduation, that is, through association with a membership function  $\mu_A$ : U [0,1], with  $\mu_A(u)$ , usU, representing the grade of membership of u in A.
- Membership in U is a matter of degree.
- In fuzzy logic everything is or is allowed to be a matter of degree.
- Fuzzy logic has nothing to do with randomness (probability),
- In essence, it deals with possibility called possibility theory.
- Mathematical objects that behave like fuzzy sets exist in probability theory. It does not mean that fuzziness is reducible to randomness.

## **Fuzzy Sets and Flexibility**



 $\mu A(x)$ : degree of belonging of x to A or degree of possessing some imprecise property represented by A

Example : tall man, long street, large number, sharp corner, very young, skin colour etc.

- Fuzzy set is a Generalization of classical set theory
- ⇒ Greater flexibility in capturing faithfully various aspects of incompleteness or imperfection in a situation.

### **Fuzzy Sets and Flexibility**

#### Meeting at 5 PM



Membership Function: Context Dependent

## **Fuzzy Sets and Flexibility**

#### **FUZZY SETS**

Flexibility of fuzzy set theory is associated with the Concept of  $\boldsymbol{\mu}$ 

- µ : A measure of compatibility of an object with the concept represented by fuzzy set.
- $\mu_{TALL} = 0.3$  means

Compatibility of some one with the set ``TALL ~ NOT the prob. that some one is TALL

i.e., 0.3 is the extent to which the concept ``TALL<sup>---</sup> must be stretched to fit him

- As µ ↑, Amount of Stretching Concept ↓
- FUZZINESS IS ANALOGOUS TO ELASTICITY

Imprecision of meaning = elasticity of meaning Elasticity of meaning = fuzziness of meaning





Fuzzy Information Granulation (FIG)

#### FIG deals with

- Imprecise representation of information,
- Problems having insufficient information.

### **Real Data set**



#### Scatter plot of VOWEL data in F1-F2 plane

#### **Fuzzy Granules**

#### Class-dependent (CD)

- Each feature explores its class belonging information to different classes,
- Features are described by the fuzzy sets (equal to the number of classes) that characterizes corresponding number of fuzzy granules along the axis.

#### Class-independent (CI)

- With CI granulation, each feature is described with some defined number fuzzy membership functions over the whole space,
- The generated granules thus, does not take care of the class belonging information of features to different classes.



Fuzzy granulation of features  $F_1$  and  $F_2$  that characterizes granules for four overlapping classes.



#### **Example of Granules Generation:**

Each feature *F* is represented by *C* (= number of classes) [0,1]-valued membership functions ( $\pi$ -type in present case) representing *C* fuzzy sets or characterizing *C* fuzzy granules along each axis; there by constituting *C<sup>n</sup>* fuzzy granules in an *n*-dimensional feature space.

#### <u>1.0</u> <u>0.5</u> <u>0.0</u>

**Figure:** Generation of granules from class-wise (class dependent) fuzzy representation of the features  $F_1$  and  $F_2$ . The figure represents the granules for four overlapping classes. The shaded regions (16 nos.) indicate the granules. For example the region (granule no 6) indicates a crisp granule obtained by  $\alpha$ -cuts ( $\alpha = 0.5$  in present case) on the  $\mu_{C_2}^1$  and  $\mu_{C_3}^2$ . The granules shape / size are variable in nature and depend on the overlapping nature of classes and class-wise feature distribution.

#### F with *n*-numeric features (F = $[F_1, F_2, ..., F_n]$ )

CI: Granulate the feature values that characterizes them in terms of some combination of membership values in the linguistic property sets *low, medium* and *high*.  $\mathbf{F} = [\mu_{low(F_1)}(F), ..., \mu_{high(F_n)}(F)]$ 

CD: Each feature is described in terms of its fuzzy membership values corresponding to L (total number of classes) linguistic fuzzy sets.Thus, an n-dimensional pattern vector is expressed as(n x L)-dimensional vector and is given by

$$\mathbf{F} = [\mu_1^1(F_1), \mu_2^1(F_1), \dots, \mu_c^1(F_1), \dots, \mu_L^1(F_1); \\ \mu_1^2(F_2), \mu_2^2(F_2), \dots, \mu_c^2(F_2), \dots, \mu_L^2(F_2); \\ \mu_1^n(F_n), \mu_2^n(F_n), \dots, \mu_c^n(F_n), \dots, \mu_L^n(F_n)] \quad (c = 1, 2, \dots, L),$$

Concept of Flexibility & Uncertainty Analysis

## Rough Sets and Information Granules : Basic Concepts

## **Historical notes**

#### **Rough sets perspectives:**

1982, Pawlak introduced the notion of rough sets.

1998, the GrC view of rough sets was discussed by many researchers (Lin, Pawlak, Skowron, Y.Y. Yao, and many more).

Rough set theory can be viewed as a concrete example of GrC.

- Offer mathematical tools to *discover* hidden patterns in data.
- Fundamental principle of a rough set-based learning system is to discover redundancies and dependencies between the given features of a data to be classified.
- Approximate a given concept both from below and from above, using lower and upper approximations.
- Rough set learning algorithms can be used to obtain rules in IF-THEN form from a *decision table*.
- Extract Knowledge from data base (decision table w.r.t. objects and attributes → remove undesirable attributes (knowledge discovery) → analyze data dependency → minimum subset of attributes (reducts))



Approximations of the set  $X \subseteq U$  w.r.t feature subset B

B-lower:  $\underline{B}X = \{x \in U : [x]_B \subseteq X\}$  Granules definitely belonging to X

**B-upper:** 
$$\overline{BX} = \{x \in U : [x]_B \cap X \neq \phi\}$$
 Granules definitely  
and possibly belonging  
to X

If BX = BX, X is B-exact or B-definable

Otherwise it is Roughly definable



### Uncertainty Handling

(Using lower & upper approximations)

**Granular Computing** (Using information granules) Granular Computing: Computation is performed using information granules and not the data points (objects)

• Information compression

Computational gain

## **Rough granulation**

Pawlak's rough set (PaRS) Neighborhood rough set (NRS)

#### **Characteristics**

NRS covers the space, and PaRS partitions,

Number of granules

- == number of patterns (NRS)
- <= number of patterns (PaRS),

### Granules shape and size (granularity of data analysis)

controlled (NRS) with two parameters, such as shape ( $\Delta$ ) and size ( $\phi$ ) not under control (PaRS)

Two neighborhood granules centered at samples  $x_1$  and  $x_2$  in F1- F2 feature space.  $\phi$  is the radius of the granules and  $\Delta(xi, xj) \le \phi$ . Granules' shape & size are determined by p-norm distance function ( $\Delta$ ) and threshold  $\phi$ .





F₁

 $\mathbf{F}_2$ 

## **Neighborhood rough granulation**

#### **Advantages**

- Significance of features vary with the granular size and granularity levels,
- Selects different feature subsets with the change of neighborhood shape and size,
- No need for feature value discretisation,
- Explores local/contextual information in an improved manner.

## **Classification model**



### **Description of the data set**

#### **Scene-region data**

- Name of the dataset: scene-regions of images (collected from Google and Flickr image data bases)
- Number of classes: 6
- Number of features: 39 (13 from each of the red-green-blue colors)
  - 6 texture features such as mean, standard deviation, smoothness, skewness, uniformity and entropy, and
  - 7 invariant moments features. These features are insensitive to translation, scale, change, mirroring and rotation.

#### Number of patterns: 700

### **Scene-region data set**



#### Four examples of scene-regions of natural images.

## **Description of the data set**

#### Image based spam-ham data

- > Name of the dataset: image based *spam-ham*
- Number of classes: 2
- Number of original features: 15
  - number of unique colors over the whole image,
  - number of text region pixels and color saturation over the whole image, and
  - color heterogeneity, color smoothness, mean and standard deviation of the images in each of the red-green-blue bands

#### Number of patterns: 1800

### Spam-Ham data set



#### Two examples of image based spam-ham data set.

### **Results (Rough-fuzzy granulation)**

#### Performance comparison of models to justify the use of

Granulated feature space,

Class-dependent (CD) fuzzy granulation,

Neighborhood rough sets (NRS) based feature selection, and

Synergistic integration of the merits of both fuzzy granulation and the theory of NRS.

Five different combinations of classification models using rough-fuzzy granular feature space and feature selection methods

model 1 (F1) : k-nearest neighbor (k-NN with k=1) classifier,

model 2 (F2): CI fuzzy granulation + k-NN (with k=1) classifier,

model 3 (F3): CD fuzzy granulation + k-NN (with k=1) classifier,

model 4 (F4): CD fuzzy granulation + PaRS based feature selection + k-NN (with k=1) classifier,

model 5 (F5): CD fuzzy granulation + NRS based feature selection + k-NN (with k=1) classifier.

Performance comparison of rough-fuzzy granulated models using 1nn classifier with scene-region data for 20% and 50% training sets.



50% training set 0.8 0.7 0.6 0.5 0.4 **Kappa** 0.2 0.2 0.1 0 3 2 5 1 4 Models 0.45 0.4 computational time 0.35 0.3 0.25 0.2 0.15 Total 0.1 0.05 0

3

Models

5

2

Note: All the simulations are done in MATLAB (Matrix Laboratory) environment in Pentium-IV machine with 3.19 GHz processor speed.

## Classification accuracies (PA) of rough-fuzzy models with different classifiers at 50% training set for scene-region data set



#### Performance comparison of rough-fuzzy granulated models using 1-nn classifier with spam-ham data for 20% and 50% training sets.



50% training set





Note: All the simulations are done in MATLAB (Matrix Laboratory) environment in Pentium-IV machine with 3.19 GHz processor speed.

## Classification accuracies (PA) of rough-fuzzy models with different classifiers at 50% training set for *spam-ham* data



### Remote sensing data set

Six classes for both IRS 1A and SPOT image data : pure water (PW), turbid water (TW), concrete area (CA), habitation (HAB), vegetation (VEG) and open spaces (OS).

### Information of RS images :

### **IRS 1A**

- size 512 x 512
- spatial resolution of 36.25 m x 36.25 m and wavelength range of 0.45-0.86 µm
- No: of bands: 4 (blue, green, red and near infrared)

### SPOT

- size 512 x 512
- spatial resolution of 20 m x 20 m and wavelength range of 0.50-0.89  $\mu m.$
- No: of bands: 3 (green, red and near infrared)

### Remote sensing data set





**(b)** 



(a) IRS-1A (band-4) enhanced image, and (b) SPOT (band-3) enhanced image

### **Results with remote sensing data set**





#### <u>(a)</u>

**(b)** 

Classified IRS-1A images with (a) model 1 and (b) model 5 (proposed model).

### **Results with remote sensing data set**





<u>(a)</u>

<u>(b)</u>

Classified SPOT images with (a) model 1 and (b) model 5 (proposed model).

### **Results with remote sensing data set**



(Zoomed) Two selected regions of classified IRS-1A image with (a and c) model 1, and (b and d) model 5

## Performance comparison of rough-fuzzy models in terms $\beta$ and DB indexes using k-NN classifier (k=1) with IRS-1A remote sensing image



Performance comparison of rough-fuzzy models in terms  $\beta$  and DB indexes using k-NN classifier (k=1) with SPOT remote sensing image (P=2, Phi=0.45)



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Performance comparison of rough-fuzzy models in terms computational time (Tc) using k-NN classifier (k=1) with IRS-1A remote sensing image

#### **Computational time (in Sec.)**



## Conclusions

- Rough-fuzzy granulated models for pattern classification are proposed, and encouraging performance was achieved with the synergetic integration of the both the granulation process,
- The advantage of neighborhood rough sets (NRS) that deal with both numerical and categorical data without any discretisation is also realized in the proposed models,
- Models with granulated feature space yielded improved performance compared to models with non-granulated feature space; justifying the use of granular computing based methods,
- NRS based feature selection method performed better than PaRS in both types of granulated models.
- Model F5 (among the rough-fuzzy granulated models) performed the best.
- Class-dependent fuzzy granulated model (F5) was superior to others with the cost of little higher value of *Tc*.