

1. Let  $G$  be a group. Prove that  $\phi : G \longrightarrow G$  given by  $\phi(g) = g^{-1}, \forall g \in G$  is an automorphism of  $G$  if and only if  $G$  is an abelian group.