

1. Let A and B be two subsets of \mathbb{R} , which are both bounded below. Let $u = \inf(A)$ and $v = \inf(B)$. Let $C = \{ab : a \in A, b \in B\}$. Is $\inf(C) = u \cdot v$?

Solution :- No.

$$A = \{-3, -2\} \quad B = \{-1, 0\} \quad \text{— are bounded below.}$$

$$\bullet \inf(A) = -3 \quad \inf(B) = -1$$

$$C = \{a \cdot b \mid a \in A, b \in B\} = \{0, 2, 3\}$$

$$\bullet \inf(C) = 0$$

$$\text{So } \inf(C) \neq \inf(A) \cdot \inf(B)$$

□