

1. Write the following statements using logical notation and negate them.

(a) Every classroom has a chair that is not broken.

(b)  $f : \mathbb{R} \rightarrow \mathbb{R}$  is unbounded if for every real number  $M$ , some real number  $x$  satisfies  $|f(x)| > M$ .

2. Define what is meant by “a sequence  $\{a_n\}_{n \geq 1}$ ”.

3. We say  $\lim_{n \rightarrow \infty} a_n = L$  if

*For every  $\epsilon > 0$  there exists  $N > 0$  such that  $|a_n - L| < \epsilon$  whenever  $n \geq N$ .*

(a) Write a logical statement that says  $\lim_{n \rightarrow \infty} a_n \neq L$

(b) Write a logical statement that says  $\lim_{n \rightarrow \infty} a_n \neq a$  for any  $a \in \mathbb{R}$ .

4. If  $f : \mathbb{R} \rightarrow \mathbb{R}$  is unbounded then construct a sequence  $\{a_n\}$  such that  $\lim_{n \rightarrow \infty} |f(a_n)| = \infty$