## Bonus Question<sup>1</sup>

Euler's constant  $\gamma$  is obtained as a limit of  $\gamma_n$  where

$$\gamma_n = \left[1 + \frac{1}{2} + \frac{1}{3} + \ldots + \frac{1}{n} - \ln n\right].$$

- (a) Provide one instance in mathematics where this  $\gamma$  appears.
- (b) Consider the use of  $\gamma_n \gamma_{n+1}$  as a convergence tolerance. From the algebraic expression for  $\gamma_n \gamma_{n+1}$  estimate how many terms are necessary to obtain a tolerance of  $5 \times 10^{-5}$ .
- (c) Write a m-file function that evaluates  $\gamma$ . Decide whether the above convegence tolerance is a good estimate of the truncation error that will occur.

<sup>&</sup>lt;sup>1</sup>Not included for this quiz and Not necessary to turn in. Prize: Slice of Black Forest cake for best answer.