

Due: Thursday February 24th 2005
Problems to be turned: 3

1. Read code of the `lupiv` function in the NMM toolbox and explain how you will use it to solve $Ax = b$.
2. Starting with the code `GEshow` in the NMM toolbox develop a `GErectangular` function that performs Gaussian elimination only for a $m \times n$ matrix. The function should return \tilde{A} , the triangularised coefficient matrix, and \tilde{b} the corresponding right hand side vector.
3. Start with the `pumpcurve` code in the NMM toolbox. It is modelling the relationship between the pressure head h of the pump and q the flow rate. Add the following features:
 - (a) Modify the `pumpcurve` function to accept q and h vectors of arbitrary length as input.
 - (b) Consider q and h from the following table:

$q(m^3/s)$	0.0001	0.00025	0.0008	0.001	0.0014
$h(m)$	115	114.2	110	105.5	92.5

Using all data points above except the fourth, use your function to find the cubic polynomial interpolant. Let c be the coefficients of the polynomial.

- (c) Replace the second point to 114 from 114.2. Do as in previous part to get \tilde{c} .
- (d) Compute
 - i. the relative difference vector $d = \frac{\tilde{c}-c}{c}$ for all i . Plot h vs q ,
 - ii. largest difference in the value of h from 100 points between $\min(q)$ and $\max q$ in both the cases.
 - iii. Plot h vs q in both the cases for the 100 points.
 - iv. Discuss the practical significance on the perturbation of h values on the coefficient c and the values of h obtained by the interpolation function.