Math 221 202	(Take home) Quiz 6 Cover-sheet	Score	
Your name	Student #		
	Due: Thursday, March 1st, 2001 at 10.	00am.	

Ground Rules:

- 1. Donot pick up a quiz for any other person.
- 2. Please turn in the quiz in person as you enter the class (no later than 10.15 am).
- 3. Open book and notes. You may consult anyone you want, but you must write up your own solutions.
- 4. Show your work. Explain your solutions clearly.
- 5. When you submit the quiz back on Tuesday, please use this cover sheet as the first page.
- 6. The grader will choose two problems randomly (page 3) and grade them.
- 7. Maximum possible score will be 25. There will be 4 points for completion and 1 point for attaching this cover sheet. No points for turning in this cover sheet without the quiz.

It would be nice if you use the space below and the back of this page to answer the problems (page 3). It will minimize my/our contributions to global warming.

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¹ Office hours: Monday 1:30pm-3pm, 5pm-6pm, Wednesday 2:30pm-3:30pm, Thursday at 1:30pm-3:00pm, Friday 11:30am-12:30pm or by appointment.

Overview of Sections 3.1,3.2,3.3

1. Vocabulary List:

- (a) Determinant.
- (b) Cofactor.
- (c) Volume and Area.

2. Key Concepts:

- (a) Determinant.
- (b) Determinant of triangular matrix, A^T , AB.
- (c) expansion of determinant along any row and column.
- (d) Relationship between elementary rows and the determinant.
- (e) Relationship between invertibility and the determinant.
- (f) Relationship between volume/area and the determinant.

3. Skills to Master:

- (a) Computing the determinant of a matrix using cofactor expansion.
- (b) Computing the determinant of a matrix using elementary operations.
- (c) Computing the area and volume using determinant.

Homework Set no.	Date	Section	Problems
Homework Set 15	February 27th	4.1	$12,\!13,\!14$
		$\frac{4.2}{4.3}$	1,6,15,27
Homework Set 16	March 1	$4.3 \\ 4.4$	5,11,13,19,23 3,7,9
		4.6	7,9,19,27

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Quiz 6 Questions

- 1. Section 3.1: 14,37
- 2. Section 3.2: 26,29,40E
- 3. Section 3.3: 23,31
- 4. Show that for a triple a, b, c with $a \neq b, a \neq c, b \neq c$ that

$$\det \begin{bmatrix} 1 & 1 & 1 \\ a & b & c \\ a^2 & b^2 & c^2 \end{bmatrix} \neq 0$$

Such a matrix is called Vandermonde matrix. Hint: Factor the resulting determinant

5. Let

$$A = \left[\begin{array}{cc} 1 & -1 \\ 1 & 3 \end{array} \right], I = \left[\begin{array}{cc} 1 & 0 \\ 0 & 1 \end{array} \right] \ .$$

- (a) Let $p(\lambda) = \det(A \lambda I)$. Show that $p(\lambda) = \lambda^2 4\lambda + 5$.
- (b) $p(\lambda) = 0$ has two solutions say λ_1, λ_2 . Find λ_1, λ_2 .
- (c) Using the values of λ_1, λ_2 that you found above, Describe a basis for the Null($A \lambda_1 I$) and Null($A - \lambda_1 I$).

 $p(\lambda)$ is called the characteristic polynomial of A. λ_1 , λ_2 are called eigen-values of A and the vectors you found in (5c) are called their eigen-vectors.

6. Let $A = \begin{pmatrix} 2 & 0 \\ 0 & 0 \end{pmatrix}$. Let $b = \begin{pmatrix} 2 \\ 1 \end{pmatrix}$. Verify Ax=b is Inconsistent. Please solve $A^T A x = A^T b$. (You should get infinitely many solutions). Pick any solution and call it x*, and let v = Ax*. systems.

Prize Question: (Need not turn in with the quiz) What is the geometric significance of the vector v? If anyone of you solves it, the whole class gets free candy. Prize offer EXTENDED-March 1.

 $Hint: \text{ Try the same calculation with say } b = \begin{pmatrix} 8 \\ 1 \end{pmatrix}.$ Then try the same calculation with say $A = \begin{pmatrix} 2 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{pmatrix}$ and $b = \begin{pmatrix} 1 \\ 1 \\ 9 \end{pmatrix}$. Sketch in each of the above three cases: b, v, range-space(A)=col(A). Spot the significance.

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