- 1. Find an example of a sequence that satisfies the below statements and then write the below statements using logical notation:
  - (a) For every  $\epsilon > 0$  there are infinitely many n such that distance of  $a_n$  to 0 is less than  $\epsilon$ .
  - (b) For every  $\epsilon > 0$  for all but finitely many n the distance of  $a_n$  to 0 is less than  $\epsilon$ .
  - (c) For every  $\epsilon > 0$ , all but finitely many elements of the sequence  $a_n$  are above  $11 + \epsilon$  and all but finitely many element are below  $5 \epsilon$ .
- 2. Provide two examples (if any) of sequences  $\{a_n\}$  that satisfy each of the statements below.
  - (a) A sequence that converges to 0 which has the property that infinitely many elements are negative numbers and infinitely many elements are positive numbers.
  - (b) A non-constant sequence that does not converge.
  - (c) For all  $\epsilon > 0$ , there are infinitely many  $n \in \mathbb{N}$  such that

$$|a_n - L| < \epsilon$$

for L = -1, 0, 3 and  $a_n \notin \{-1, 0, 3\}$  for infinitely many  $n \in \mathbb{N}$ .

- (d) A sequence that converges to 0 which has the property that all but finitely many elements are negative.
- (e) For all  $\epsilon > 0$ , for all but finitely many  $n \in \mathbb{N}$   $a_n < 5 + \epsilon$  and  $a_n > -11 \epsilon$ .
- (f) For all M > 0: there are infinitely many  $n \in \mathbb{N}$  such that  $a_n > M$  and there are infinitely many  $n \in \mathbb{N}$  such that  $a_n < -M$ .
- 3. If  $f:\mathbb{R}\to\mathbb{R}$  is unbounded then construct a sequence  $\{a_n\}$  such that  $\lim_{n\to\infty} |f(a_n)|=\infty$
- 4. It is important to understand the logical implication of  $(P \Longrightarrow Q \text{ along with the operations of the Converse } (Q \Longrightarrow P)$ , the Contrapositive  $(\neg Q \Longrightarrow \neg P)$  and the negated implication  $\neg P(\Longrightarrow Q)$ . Please fill in the truth table below to illustrate the differences between these operations:

P	Q	$P \Longrightarrow Q$	$Q \Longrightarrow P$	$\neg Q \Longrightarrow \neg P$	$\neg(P \Longleftrightarrow Q)$
Т	Т				
Т	F				
F	Т				
F	F				