

$I$  - treatments and  $J$ - population in each treatment.

**Model:**  $y_{ij} = \mu + \alpha_i + \epsilon_{ij}$  with errors  $\epsilon_{ij}$  being independent Normal  $(0, \sigma^2)$  and differential effect  $\sum_{i=1}^I \alpha_i = 0$

**Null Hypothesis:**  $\alpha_1 = \alpha_2 = \dots = \alpha_I = 0$

**Alternative Hypothesis:** One of the  $\alpha_i$  differ from 0.

$I$  - treatments and  $J$ - population in each treatment.

$$\begin{aligned} \text{Total Sum of squares} &:= \sum_{i=1}^I \sum_{j=1}^J (y_{ij} - \bar{y})^2 \\ &= \sum_{i=1}^I \sum_{j=1}^J (y_{ij} - \bar{y}_{i\cdot})^2 + J \sum_{i=1}^I (\bar{y}_{i\cdot} - \bar{y})^2 \\ &:= \text{Sum of squares within treatment groups} \\ &\quad + \text{Sum of squares between treatment groups} \end{aligned}$$

In Short:

$$SS_{\text{total}} = SS_W + SS_B$$

$I$  - treatments and  $J$ - population in each treatment.

Test Statistic:

$$F := \frac{SS_B / (I - 1)}{SS_W / (I(J - 1))}$$

where  $F \sim F(I - 1, I(J - 1))$

Decide on  $\alpha$

Calculate  $p$ -value :  $= P\left(F(I - 1, I(J - 1)) > \frac{SS_B / (I - 1)}{SS_W / (I(J - 1))}\right)$

**Reject Null Hypothesis** if  $p$ -value is less than  $\alpha$

1. Execute a `for loop` in R via the following code.

```
> for (i in 1:10) {
+   if (!i %% 2){
+     next
+   }
+   print(i)
+ }
```

```
[1] 1
[1] 3
[1] 5
[1] 7
[1] 9
```

Describe what it is doing.

2. Use the `searchtimes.csv`, `firingrate.csv` from (Sripati and Olson 2010) data.

- (a) Using `read.csv` with additional option `skip = 2` read the above datasets into R, as variables `S` and `F`.

```
> S= read.csv("searchtimes.csv", skip=2, header=TRUE)
> F= read.csv("firingrates.csv", skip=2, header=TRUE)
```

- (b) From the 18 column ( 9 corresponding pairs of images) in the dataset `firingrates.csv` using the `for loop` compute the  $L_1$  distance<sup>1</sup> between the firing rates across the pairs. Assign variable `LONE` for this data (it should be a vector of length 9).

```
> LONE = rep(1:18)
> for(i in 1:9){ LONE[i] = sum(abs(F[,2*i-1]-F[,2*i]))}
> LONE = LONE/114
```

- (c) Deduce what this code achieves.

```
> RLONE = replicate(2, LONE)
> FLONE = c(t(RLONE))
```

- (d) There should be 18 columns in for each image pair, providing the search times. Convert `S` into search delays by subtracting the baseline reaction time of 328 ms and store it in `SD`.

- (e) Deduce what this code achieves

```
> SD= S-328
> STSD = SD*FLONE
```

- (f) Deduce what this code achieves

```
> n = rep(72,18)
> group = rep(1:18,n)
> VSTSD = unlist(STSD, use.names=FALSE)
> AOVDATA = data.frame(y = VSTSD, group = factor(group))
```

- (g) Using the `oneway.test` to test whether all the 18 image pairs  $E[s_{ij}LONE_{ij}]$  is the same. Please justify your answer.

```
> oneway.test(y~group, data=AOVDATA, var.equal=TRUE)
```

One-way analysis of means

```
data: y and group
F = 9.4655, num df = 17, denom df = 1278, p-value < 2.2e-16
```

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<sup>1</sup>for vectors  $x_1, x_2, \dots, x_n$  and  $y_1, y_2, \dots, y_n$  we shall designate the  $L_1$  distance by  $\frac{1}{n} \sum_{i=1}^n |x_i - y_i|$