

1. Let K be a compact subset of \mathbb{R}^n . Prove given $\epsilon > 0$ that there is a C^∞ function $\rho_K(\cdot)$ on \mathbb{R}^n such that

$$\rho_K(\mathbb{R}^n) \subset [0, 1], \quad \text{supp}(\rho_K) \subset \{y \in \mathbb{R}^n : \text{Dist}(y, K) < \epsilon\}, \quad \text{and} \quad \rho_K \equiv 1 \text{ on } K.$$