

Erdős Renyi Graph $G(n, p)$ is constructed in the following manner:

1. Consider n vertices labeled $\{1, 2, \dots, n\}$.
2. Corresponding to each distinct pair $\{i, j\}$ we perform an independent Bernoulli (p) experiment and insert an edge between i and j with probability p . Note that all edges are *undirected* and hence there are total of $\binom{n}{2}$ possible edges, each occurring with probability p .

3. In this group worksheet you will simulate an Erdős Renyi Graph and find the M.L.E. for the relevant p . Your groups are available at:

<https://docs.google.com/spreadsheets/d/1dqH5BvvYID43fK0Syx29CMFvo4hlyQvDcg0iReaO-Ns/edit?usp=sharing>

1. Choosing x : Write a simple R-code to generate a number uniformly from $\{1, 2, 3, 4, 5\}$. Let x denote the chosen number. Record x in the box:

2. Consider the experiment of rolling a die and (choose) specify an event from that experiment which occurs with probability $x/6$. *All three persons together* decide on that event, and let it be called B . Write out the description of the event B in the box below:

3. The set of vertices for the graph you are about to construct are $\{1, 2, \dots, 10\}$. The graph has no self-edges (i.e Self-loops). What is the total number of possible edges ?

Record answer in the box:

4. Construct the *random* adjacency matrix A for the graph as follows. For each pair $1 \leq i < j \leq 10$:

- (a) Roll your die(using one at home or at <http://www.randomservices.org/random/apps/Dice.html>) and observe if the event B has occurred.

(Take turns with each person Rolling the die 15 times.)

- (b) Designate

$$a_{ij} = \begin{cases} 1 & \text{if } B \text{ occurred.} \\ 0 & \text{if } B \text{ did not occur} \end{cases}$$

All three persons in respective sheets fill in the matrix entries accordingly:

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5. Using the **igraph** package draw the random graph, denote by $G(10, \frac{x}{6})$, corresponding to the above adjacency matrix (i.e draw an edge between i and j if $a_{ij} = 1$).