

For numerical answers with decimal digits please read instructions.

1. Let $X \sim \text{Poisson}(100)$ then
 - (a) $\mathbb{E}[3 + X]$ is _____.
 - (b) $\text{SD}[4X]$ is _____.
2. Suppose we toss a fair coin till we obtain 10 heads. Let X denote the trial at which this occurs. Then
 - (a) $\mathbb{E}[X]$ is _____.
 - (b) $\text{Var}[X]$ is _____.
3. Let $X \sim \text{Geometric}(\frac{1}{4})$.
 - (a) $\mu := \mathbb{E}[X] =$ _____.
 - (b) The probability that X will be within one standard deviation of average is _____.
Give your answer rounded up to four decimal digits.
4. Let m and r be positive integers and let N be an integer for which $N > \max\{m, r\}$. Let X be a random variable with $X \sim \text{HyperGeo}(N, r, m)$. Then which of the following is true:
 - i. $\mathbb{E}[X] = \frac{mr}{N}$ and $\mathbb{E}[X^2] = \frac{mr}{N} + \frac{mr(m-1)(r-1)}{N(N-1)}$
 - ii. $\mathbb{E}[X] = \frac{r}{N}$ and $\mathbb{E}[X^2] = \frac{r}{N} + \frac{m^2 r^2}{N(N-1)}$
 - iii. $\mathbb{E}[X] = \frac{r}{N+r}$ and $\mathbb{E}[X^2] = \frac{r}{N+r} + \frac{m^2 r^2}{N(N-1)+r(r-1)}$
 - iv. $\mathbb{E}[X] = \frac{N}{r}$ and $\mathbb{E}[X^2] = \frac{N}{r} + \frac{N(N-1)}{m^2 r^2}$
5. Let X, Y be discrete random variables. Suppose $X \leq Y$ then it is possible that:
 - i $\mathbb{E}[X] \leq \mathbb{E}[Y]$
 - ii $\mathbb{E}[X] > \mathbb{E}[Y]$
6. A random variable X has a probability mass function given by

$$\mathbb{P}(X = 0) = 0.2, \mathbb{P}(X = 1) = 0.5, \mathbb{P}(X = 2) = 0.2, \text{ and } \mathbb{P}(X = 3) = 0.1.$$
 - (a) $\mathbb{E}[X]$ is _____.
Give your answer rounded up to one decimal digit.
 - (b) $\text{SD}[X]$ is _____.
Give your answer rounded up to four decimal digits.
 - (c) The probability X will produce a result more than one standard deviation from its expected value is _____.
Give your answer rounded up to one decimal digit.

7. Suppose we choose a number uniformly from $\{1, 2, 3, 4, 5, 6\}$. Let X be the number chosen. Then $\mu := \mathbb{E}[X] = \underline{\hspace{1cm}}$.
Give your answer rounded up to one decimal digit.