

Indian Statistical Institute, Bangalore  
MS (QMS) First Year  
Second Semester - Advanced Statistical Process Control

Midterm Exam  
Maximum marks: 60

Date: April 24, 2023  
Duration: 3 hours

1. [4 + 10 + 2 = 16]

a) Define the procedure for item-by-item sequential sampling plan.

b) Derive the item-by-item sequential sampling plan for

$$\alpha = 0.05, p_1 = 0.02, \beta = 0.10, p_2 = 0.15$$

(Write down all necessary formulas for calculation).

If the reference single sampling plan is  $n = 75, c = 3$ ; suggest the multiple sampling plan.

2. [3 + 12 = 15]

a) Explain the need for chain sampling plan.

b) Calculate AQL, LTPD, AOQL values for the plan

i)  $n = 5, c = 0$  and

ii)  $n = 5, i = 2$  (chain sampling plan)

(Write down necessary formulas used for calculation, compare the plans?)

3. [5 + 10 + 10 + 4 = 29]

a) Explain how to implement Taguchi's  $\beta$ -correction method.

b) Derive the  $\beta$ -correction factor for a continuous characteristics in a manufacturing process.

c) Compute the  $\beta$ -correction formula by using the following data.

5.204, 5.204, 5.217, 5.208, 5.221, 5.200, 5.221, 5.221, 5.213, 5.218, 5.218, 5.230, 5.239, 5.239, 5.300, 5.323

(Write down all calculation including the ANOVA tables)

d) If the tolerance of the dimension is  $5.230 \pm 0.01$ ; suggest the range of no correction.

4. [3 + 5 + 2 = 10]

a) Illustrate the CSP\_1, CSP\_2 and CSP\_3 plans.

b) Compute the AOQL value for the following CSP\_1 plan  $i = 50, f = \frac{1}{3}$ .

c) Compare the above CSP\_1 plan with the single sampling plan  $n = 5, c = 0$ .

(Write all formulas and calculation).