# Indian Statistical Institute, Bangalore 

MS (QMS) First Year
Second Semester - Advanced Statistical Process Control

Back Paper Exam
Date: Jun 13, 2019
Maximum marks: 100
Duration: 3 hours
1.

$$
[5+15=20]
$$

a) Specify the conditions, under which a group control chart can be established in a process.
b) A machine has four heads. Samples of $n=5$ units are selected from each head, and $\bar{x}$ and $R$ values of the characteristic are computed. Setup group control chart for this process.

## Head

| Sample No. | 1 |  | 2 |  | 3 |  | 4 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\bar{x}$ | $R$ | $\bar{x}$ | $R$ | $\bar{x}$ | $R$ | $\bar{x}$ | $R$ |
| 1 | 23 | 2 | 24 | 1 | 26 | 2 | 23 | 3 |
| 2 | 21 | 1 | 23 | 2 | 22 | 4 | 24 | 4 |
| 3 | 24 | 2 | 22 | 5 | 23 | 3 | 27 | 2 |
| 4 | 35 | 3 | 24 | 3 | 22 | 1 | 21 | 5 |
| 5 | 24 | 1 | 20 | 2 | 21 | 1 | 23 | 1 |
| 6 | 23 | 2 | 21 | 1 | 24 | 2 | 22 | 2 |
| 7 | 21 | 1 | 23 | 2 | 28 | 5 | 24 | 1 |
| 9 | 22 | 2 | 24 | 4 | 21 | 2 | 25 | 2 |
| 10 | 20 | 2 | 22 | 3 | 22 | 1 | 21 | 3 |
| 9 | 21 | 1 | 25 | 1 | 23 | 3 | 23 | 5 |

2. Prepare a short run version of c-chart for the given 100\% inspection data of a component.

| Sample No. | Variety | No. Impacted | No. Rejected |
| :---: | :---: | :---: | :---: |
| 1 | A | 240 | 22 |
| 2 | B | 236 | 13 |
| 3 | B | 137 | 9 |
| 4 | C | 421 | 33 |
| 5 | D | 329 | 17 |


| 6 | A | 210 | 15 |
| :---: | :---: | :---: | :---: |
| 7 | B | 410 | 18 |
| 8 | B | 323 | 24 |
| 9 | C | 323 | 29 |
| 10 | B | 167 | 7 |

3. Write short notes on (any four):-
a) SPC implementation
b) $\mathrm{SPC} v / \mathrm{s}$ EPC
c) Dominance System
d) Chain Sampling
e) Taguchi concept of loss function
4. 

a) State the $\beta$-correction procedure.
b) Derive the $\beta$-correction factor.
c) State the Control method.
5. Compute the $\beta$-correction table from the consecutive 16 observation for the product characteristic $25 \pm 5 \mathrm{~mm}$.
$25,20,20,20,25,25,27,25,22,22,28,25,25,28,28,30$.
6.

$$
[10+5=15]
$$

a) State the continuous sampling methods (csp-1, csp-2, csp-3).
b) Compute the $P(A)$ for the quality $p-0.01$ and 0.015 for the $\operatorname{csp}$ plan $i=50, f=\frac{1}{3}$.
7. Calculate the probability of acceptance for a chain sampling plan for the following lot quality $p=0.005,0.01$ and 0.015 .

