

**Indian Statistical Institute, Bangalore**  
**M.S. (QMS) First Year**  
**Second Semester – Statistics for Decision Making II**

Final Exam      Duration: 3 Hrs      Date: May 04, 2017      Max Marks: 50

*Answer as many questions as you can, but the maximum score you can get is 50 only.*

1. For the One Way ANOVA, consider the fixed effect model  $y_{ij} = \mu + \alpha_i + \varepsilon_{ij}$ , ( for all  $i=1,2,\dots,a$  &  $j=1,2,\dots,n$ ), where ,  
 $\mu$  = Overall Population mean,  
 $\alpha_i$  = Effect of the  $i$ th class of attribute A,(  $i=1,2,\dots,a$ ) and  
 $\varepsilon_{ij}$  = Error for the  $j$ th observation in the  $i$ th class(  $j=1,2,\dots,n$ ), and  
 $\varepsilon_{ij}$ 's ( for each  $i=1,2,\dots,a$  &  $j=1,2,\dots,n$ ) are independently normally distributed with zero mean and constant variance =  $\sigma^2$ .

$$\text{Show that } E(\text{MSA}) = \sigma^2 + n \left( \frac{\sum_{i=1}^a \alpha_i^2}{a-1} \right) \quad [10]$$

2. Show that  $-1 \leq r \leq 1$ , where 'r' is the correlation coefficient between two variables x and y . [10]
3. It is known that a sample consisting of the values 11.5, 11.2, 13.5, 12.3, 13.8, and 11.9 comes from a population with the density function

$$f(x; \theta) = \frac{\theta}{x^{\theta+1}}$$

=0, elsewhere,

where  $\theta > 0$ . Find the maximum likelihood estimate of  $\theta$ . [8]

**or**

Ten engineering colleges in India were surveyed. The sample contained 250 electrical engineers, 80 being women; 175 chemical engineers, 40 being women.

- (a) Compute a 90% confidence interval for the difference between the proportions of women in these two fields of engineering.
- (b) Is there a significant difference between the two proportions? [6+2=8]
4. Engineers at a large automobile manufacturing company are trying to decide whether to purchase brand A or brand B tyres for the company's new models. To help the arrive at a decision, an experiment is conducted using 12 of each brand. The tyres are run until they wear out. The results are as follows:

Brand A:  $\bar{x}_1 = 37,900$  kilometers,  $s_1 = 5100$  kilometers.

Brand B:  $\bar{x}_2 = 39,800$  kilometers,  $s_2 = 5900$  kilometers.

Test the hypothesis that there is no difference in the average wear of the two brands of tyres. Assume the populations to be approximately normally distributed with equal variances. [10]

5. The grades of a class of 9 students on a midterm report ( $x$ ) and on the final examination ( $y$ ) are as follows:

$x$ : 77 50 71 72 81 94 96 99 67

$y$ : 82 66 78 34 47 85 99 99 68

- (a) Estimate the linear regression line.  
 (b) Estimate the final examination grade of a student who received a grade of 85 on the midterm report. [8+2=10]

6. An experiment was conducted to study the effects of temperature and type of oven on the life of a particular component. Two types of ovens and 3 temperature levels were used in the experiment. Twelve pieces were assigned randomly, two to each combination of treatments, and the following results recorded.

Temperature	OVEN	
	1	2
500	227, 221	214, 259
550	187, 208	181, 179
600	174, 202	198, 194

Analyze the data and draw conclusions (use  $\alpha = 0.05$ ).

[12]