# INDIAN STATISTICAL INSTITUTE SQC \& OR Unit, Hyderabad <br> MS in Quality Management Science: 2015-17 <br> III SEMESTER: FINAL EXAMINATION 

Subject: Applied Regression Analysis (ARA)
Date: 7 November 2016
Duration: 3 Hours
Max. Marks: 100

## INSTRUCTIONS

This paper contains questions for 120 marks. Answer as many as you can but the maximum you can score is 100 marks. You will also be given soft copy of this question paper for using data for analysis. You are free to use appropriate statistical software for analysis but the answers will have to be given in the answer sheet given to you. You need to also submit the soft copy of your analysis if any, only in a word file format opened in your name before the end of the examination without fail.

Q1. Answer any five of the following. Your answer should be brief (Max. 20 lines) and you may use examples wherever relevant.
a. Different variable selection methods in a multiple regression set up highlighting criteria used in variable selection in each method. Also, mention the salient merits and demerits of each method.
b. Methods to handle multi collinearity among regressors. Also, mention the salient merits and demerits of each method.
c. Methods to handle non-linearity in modelling and mention the main significant difference of these methods over traditional linearization approaches.
d. Practical significance of validation in regression modelling and list commonly adopted validation methods with significance of each method.
e. Measures for checking the model adequacy in a multiple regression set up and salient merits and/or demerits of each measure.
f. Role of different classification and tree based methods in modelling and main criterion used in each method.
g. How outliers influence model adequacy and list different methods to handle outliers in the data while modelling. Specify the decision criteria used in each method.

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[5 \mathrm{X} 10=50 \text { Marks }]
$$

Q2. Following table contains the data on Exports in Tons of Production made by a company during the 2007-12.
a) Fit an appropriate forecasting model to the data and give the quarter wise forecast along with the suitable prediction interval for the next two years.
b) Explain the criteria you have adopted in building and selecting the final model.
c) Also find the AIC and BIC estimates for each of the models you have tried in questions a) \& b) above and explain how you would use these criterions in your final model selection.
$[10+5+10=25$ Marks $]$

| Year | Quarter | Period | Exports <br> in Tons |
| :--- | :--- | :--- | :--- |
|  | Apr | 1 | 362 |
|  | Jul | 2 | 385 |
|  | Oct | 3 | 432 |
|  | Jan | 4 | 341 |
| 2008 | Apr | 5 | 382 |
|  | Jul | 6 | 409 |
|  | Oct | 7 | 498 |
|  | Jan | 8 | 387 |
| 2010 | Apr | 9 | 473 |
|  | Jul | 10 | 513 |
|  | Oct | 11 | 582 |
|  | Jan | 12 | 474 |
| 2011 | Apr | 13 | 544 |
|  | Jul | 14 | 582 |
|  | Oct | 15 | 681 |
|  | Jan | 16 | 557 |
| 2012 | Apr | 17 | 628 |
|  | Jul | 18 | 707 |
|  | Oct | 19 | 773 |
|  | Jan | 20 | 592 |
|  | Apr | 21 | 627 |
|  | Jul | 22 | 725 |
|  | Oct | 23 | 854 |
|  | Jan | 24 | 661 |

Q3. The following is the data on Cost of Healthcare which was collected by the Department of Health and Social Services of the State of New Mexico and cover 52 of the 60 licensed facilities in New Mexico in 1988. The variables in the data are the characteristics which describe the facilities size, volume of usage, expenditures and revenue. The location of the facility is indicated whether it is in the rural or non-rural area.
i) Using the data given, build a logistic regression model to understand whether the rural facilities are different from non-rural facilities. List the model adequacy
measures that need to be used in logistic modelling and verify the model adequacy of the developed model.
ii) Also, build an appropriate model for patient care revenue using hospital characteristics. Comment on the adequacy of the model developed by using appropriate diagnostic measures.
iii) Estimate the AIC and BIC for models tried and comment on the adequacy of the model selected in both cases using these criteria.

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[15+15+15=45 \text { Marks }]
$$

| Variable | Description |
| :--- | :--- |
| RURAL | Rural home (1) and Non-rural home (0) |
| BED | Number of Beds in home |
| MCDAYS | Annual medical in-patient days (hundreds) |
| TDAYS | Annual total patient days (hundreds) |
| PCREV | Annual total patient care revenue (\$100) |
| NSAL | Annual nursing salaries (\$100) |
| FEXP | Annual facilities expenditures (\$100) |
| NETREV | PCREV-NSAL-FEXP |


| RURAL | BED | MCDAYS | TDAYS | PCREV | NSAL | FEXP | NETREV |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 0 | 244 | 128 | 385 | 23521 | 5230 | 5334 | 12957 |
| 1 | 59 | 155 | 203 | 9160 | 2459 | 493 | 6208 |
| 0 | 120 | 281 | 392 | 21900 | 6304 | 6115 | 9481 |
| 0 | 120 | 291 | 419 | 22354 | 6590 | 6346 | 9418 |
| 0 | 120 | 238 | 363 | 17421 | 5362 | 6225 | 5834 |
| 1 | 65 | 180 | 234 | 10531 | 3622 | 449 | 6460 |
| 1 | 120 | 306 | 372 | 22147 | 4406 | 4998 | 12743 |
| 1 | 90 | 214 | 305 | 14025 | 4173 | 966 | 8886 |
| 0 | 96 | 155 | 169 | 8812 | 1955 | 1260 | 5597 |
| 1 | 120 | 133 | 188 | 11729 | 3224 | 6442 | 2063 |
| 0 | 62 | 148 | 192 | 8896 | 2409 | 1236 | 5251 |
| 1 | 120 | 274 | 426 | 20987 | 2066 | 3360 | 15561 |
| 0 | 116 | 154 | 321 | 17655 | 5946 | 4231 | 7478 |
| 1 | 59 | 120 | 164 | 7085 | 1925 | 1280 | 3880 |
| 1 | 80 | 261 | 284 | 13089 | 4166 | 1123 | 7800 |
| 1 | 120 | 338 | 375 | 21453 | 5257 | 5206 | 10990 |
| 1 | 80 | 77 | 133 | 7790 | 1988 | 4443 | 1359 |
| 1 | 100 | 204 | 318 | 18309 | 4156 | 4585 | 9568 |
| 1 | 60 | 97 | 213 | 8872 | 1914 | 1675 | 5283 |
| 1 | 110 | 178 | 280 | 17881 | 5173 | 5686 | 7022 |


| 0 | 120 | 232 | 336 | 17004 | 4630 | 907 | 11467 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 0 | 135 | 316 | 442 | 23829 | 7489 | 3351 | 12989 |
| 1 | 59 | 163 | 191 | 9424 | 2051 | 1756 | 5617 |
| 0 | 60 | 96 | 202 | 12474 | 3803 | 2123 | 6548 |
| 1 | 25 | 74 | 83 | 4078 | 2008 | 4531 | -2461 |
| 1 | 221 | 514 | 776 | 36029 | 1288 | 2543 | 32198 |
| 1 | 64 | 91 | 214 | 8782 | 4729 | 4446 | -393 |
| 0 | 62 | 146 | 204 | 8951 | 2367 | 1064 | 5520 |
| 1 | 108 | 255 | 366 | 17446 | 5933 | 2987 | 8526 |
| 1 | 62 | 144 | 220 | 6164 | 2782 | 411 | 2971 |
| 0 | 90 | 151 | 286 | 2853 | 4651 | 4197 | -5995 |
| 0 | 146 | 100 | 375 | 21334 | 6857 | 1198 | 13279 |
| 1 | 62 | 174 | 189 | 8082 | 2143 | 1209 | 4730 |
| 1 | 30 | 54 | 88 | 3948 | 3025 | 137 | 786 |
| 0 | 79 | 213 | 278 | 11649 | 2905 | 1279 | 7465 |
| 1 | 44 | 127 | 158 | 7850 | 1498 | 1273 | 5079 |
| 0 | 120 | 208 | 423 | 29035 | 6236 | 3524 | 19275 |
| 1 | 100 | 255 | 300 | 17532 | 3547 | 2561 | 11424 |
| 1 | 49 | 110 | 177 | 8197 | 2810 | 3874 | 1513 |
| 1 | 123 | 208 | 336 | 22555 | 6059 | 6402 | 10094 |
| 1 | 82 | 114 | 136 | 8459 | 1995 | 1911 | 4553 |
| 1 | 58 | 166 | 205 | 10412 | 2245 | 1122 | 7045 |
| 1 | 110 | 228 | 323 | 16661 | 4029 | 3893 | 8739 |
| 1 | 62 | 183 | 222 | 12406 | 2784 | 2212 | 7410 |
| 1 | 86 | 62 | 200 | 11312 | 3720 | 2959 | 4633 |
| 1 | 102 | 326 | 355 | 14499 | 3866 | 3006 | 7627 |
| 0 | 135 | 157 | 471 | 24274 | 7485 | 1344 | 15445 |
| 1 | 78 | 154 | 203 | 9327 | 3672 | 1242 | 4413 |
| 1 | 83 | 224 | 390 | 12362 | 3995 | 1484 | 6883 |
| 0 | 60 | 48 | 213 | 10644 | 2820 | 1154 | 6670 |
| 1 | 54 | 119 | 144 | 7556 | 2088 | 245 | 5223 |
| 0 | 120 | 217 | 327 | 20182 | 4432 | 6274 | 9476 |
|  |  |  |  |  |  |  |  |

